Can you apostille a passport?

Yes and no.

You can't per se apostille a passport but you can apostille a properly notarized certified copy affidavit that gets attached to a color photocopy of a passport at one of the fifty secretaries of state in the United States.